Simulation Study of Energetic Ion Distribution during Combined NBI and ICRF Heating in LHD

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ICRF Heating Experiment in LHD

ICRF heating experiments have been ٠ successfully done and have shown significant performance (steady state experiments) of this heating method in LHD.

(Fundamental harmonic minority heating)

Up to 800keV of energetic tail ions have been ۲ observed by NDD-NPA.









Perpendicular NBI and 2nd Harmonic ICRF Heating

- Higher harmonic heating is efficient for the energetic particle generation.
 (Acceleration, Δv_{perp}, is proportional to J_n)
- The perpendicular injection NBI has been installed in LHD (2005).
 NBI#4 P < 3MW (<6MW), E= 40keV
- The perp. NBI beam ions would enhance the 2nd-harmonics ICRF heating (high init. E).
- We investigate the combined heating of perp. NBI and 2nd-harmonics ICRF.





ICRF Heating in Helical Systems

- ICRF heating generates highly energetic tail ions, which drift around the torus for a long time (typically on a collisional time scale).
- Thus, the behavior of these energetic ions is strongly affected by the characteristics of the drift motions, that depend on the magnetic field configuration.
- In particular, in a 3-D magnetic configuration, complicated drift motions of trapped particles would play an important role in the confinement of the energetic ions and the ICRF heating process.
 - Global simulation is necessary!





ICH+NBI Simulation Model by GNET

• We solve the drift kinetic equation as a (time-dependent) initial value problem in 5D phase space based on the Monte Carlo technique.

$$\frac{\partial f_{beam}}{\partial t} + (\mathbf{v}_{//} + \mathbf{v}_{D}) \cdot \nabla f_{beam} + \mathbf{a} \cdot \nabla_{\mathbf{v}} f_{beam} - C(f_{beam}) - Q_{xcr}(f_{beam}) - L_{particle} = S_{beam}$$

$$C(f) : \text{linear Clulomb Collision Operator}$$

$$Q_{ICRF} : \text{ICRF heating term} \\ \text{wave-particle interaction model}$$

$$S_{beam} : \text{beam particle source} \\ => \text{ by NBI beam ions} \\ (\text{HFREYA code})$$

$$L_{particle} : \text{particle sink (loss)} \\ => \text{ Charge exchange loss} \\ => \text{ Orbit loss (outermost flux surface)}$$
The energetic beam ion distribution f_{beam} is evaluated through a convolution of S_{beam} with a characteristic



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time dependent Green function, **G**.

Monte Carlo Simulation for **G**

- Complicated particle motion
 Eq. of motion in the Boozer coordinates (ψ,θ,φ,ρ)
 3D MHD equilibrium (VMEC+NEWBOZ)
- Coulomb collisions

Liner Monte Carlo collision operator [Boozer and Kuo-Petravic] Energy and pitch angle scattering

$$C^{coll}(\delta f) = \frac{1}{v^2} \frac{\partial}{\partial v} \left[v^2 v_E \left(v \, \delta f + \frac{T}{m} \frac{\partial \delta f}{\partial v} \right) \right] + \frac{v_d}{2} \frac{\partial}{\partial \lambda} \left(1 - \lambda^2 \right) \frac{\partial \delta f}{\partial \lambda}, \quad \lambda = \frac{v_{ll}}{v}$$

• The *Q_{ICRF}* term is modeled by the Monte Carlo method. When the test particle pass through the resonance layer the perpendicular velocity of this particle is changed by the following amount

$$\begin{aligned} \Delta \mathbf{v}_{\perp} &= \sqrt{\left(\mathbf{v}_{\perp 0} + \frac{q}{2m}I\left(\underline{E}_{+}\left(J_{n-1}(k_{\perp}\rho)\,\cos\phi_{r}\right)^{2} + \frac{q^{2}}{4m^{2}}\left\{I\left(\underline{E}_{+}\left(J_{n-1}(k_{\perp}\rho)\right)^{2}\,\sin^{2}\phi_{r} - \mathbf{v}_{\perp 0}\right)\right\}^{2} \sin^{2}\phi_{r} - \mathbf{v}_{\perp 0}\right\} \\ &\approx \frac{q}{2m}I\left(\underline{E}_{+}\left(J_{n-1}(k_{\perp}\rho)\,\cos\phi_{r} + \frac{q^{2}}{8m^{2}\mathbf{v}_{\perp 0}}\left\{I\left(\underline{E}_{+}\left(J_{n-1}(k_{\perp}\rho)\right)^{2}\,\sin^{2}\phi_{r}\right)\right)^{2} \sin^{2}\phi_{r}\right\} \\ &I = \min(\sqrt{2\pi/n\dot{\omega}}\,,\,2\pi(n\ddot{\omega}/2)^{-1/3}Ai(0)\,) \end{aligned}$$



RF Electric Field by TASK/WM



Beam Ion Distribution of Perp. NBI w/o ICH (v-space)

Perp. NBI beam ion distribution R_{ax}=3.60m $T_{eo} = T_{io} = 3.0 \text{keV}, n_{e0} = 2.0 \times 10^{19} \text{m}^{-3}, E_b = 40 \text{keV}$



- Higher distribution regions can be seen near the beam sources (E₀, E_{1/2}, E_{1/3}). (*left: lower level, right: higher level and cutting at r/a=0.8*)
- The beam ion distribution shows slowing down and pitch angle diffusion in velocity space.

Beam Ion Distribution of Perp. NBI w/o ICH



 Iso-surface plots of beam ion distribution without ICH in the 3D space, (E, pitch angle, r/a). *(left: higher level, right: lower level)*



The beam ion distribution shows slowing down and pitch angle diffusion.

Beam Ion Distribution with 2nd Harmonics ICH







Beam Ion Pressure Profile with 2nd Harmonics ICH



$$p_{beam} = 2\pi \int \frac{1}{2} m v^2 f(v_{//}, v_{\perp}) dv_{//} v_{\perp} dv_{\perp}$$

 $T_{eo} = T_{io} = 1.6 \text{ keV},$ $n_{e0} = 1.0 \times 10^{19} \text{ m}^{-3}$ B = 2.75 T @ R = 3.6 m, $f_{\text{RF}} = 76.94 \text{ MHz}, k_{//} = 5 \text{m}^{-1},$ $k_{\text{perp}} = 62.8 \text{m}^{-1}$



Simulation of NDD-NPA (2nd ICRF+NBI)



- We have simulated the NDD-NPA using the GNET simulation results.
- The tail ion energy is enhanced to MeV order and a larger tail formation can be seen than that of the fundamental harmonic heating case.



Summary

- We have been developing an ICRF heating simulation code in toroidal plasmas using two global simulation codes: TASK/WM(a full wave field solver in 3D) and GNET(a DKE solver in 5D).
- The GNET (+TASK/WM) code has been applied to the analysis of ICRF heating in the LHD (2nd-harmonic heating with perp. NBI).
- A steady state distribution of energetic tail ions has been obtained and the characteristics of distributions in the real and phase space are clarified.
- The GNET simulation results of the combined heating of the perp. NBI and 2nd-harmonic ICRF have shown effective energetic particle generation in LHD
- The benchmarking with ORBIT-RF has been done assuming C-Mod plasma and preliminary results have been shown.
- Self-consistent analysis including the effect of energetic ion distribution on the fast wave propagation by TASK code is under way.

