

Applications of Monte Carlo method in Spallation Physics

Harphool Kumawat
Nuclear Physics Division, BARC

Introduction of spallation reaction mechanism

Physics Models

Intra-nuclear cascade model

Pre-equilibrium (exciton model)

Evaporation (Generalized Evaporation Model)

Fission model (Fong's Model)

Realization of the physics models in real problem

Define Geometry

Ionization loss

Tracing till stop/exit

Intra-Nuclear Cascade model

What are the inputs we have?

Projectile:

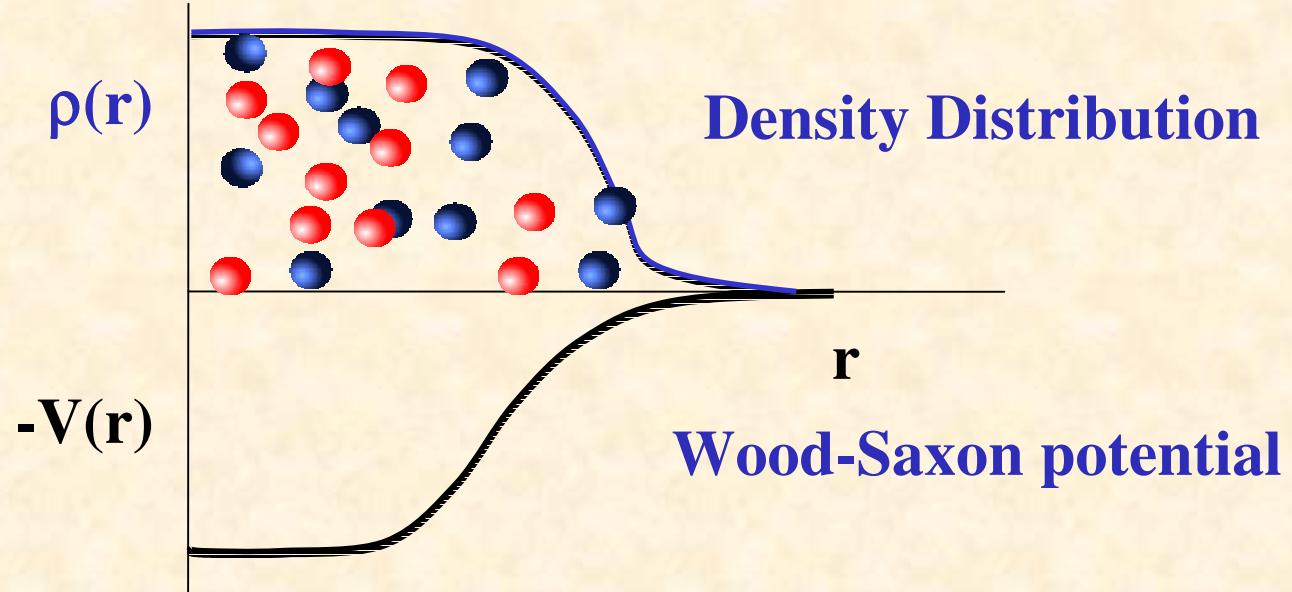
Target:



Charge, mass, energy/momentum

Charge, mass, nucleon density distribution

Each nucleon is assigned position & momentum
Using Random Numbers



$$\left\{ \begin{array}{l} \rho(r) = \frac{\rho_0}{1 + \exp \frac{(r - r_0)}{a}} \\ \text{where } r_0 = 1.07 A^{1/3} fm \\ a = 0.545 fm \\ \rho(r) = \rho_0 \exp \frac{-r^2}{R^2} \quad \text{For } A \leq 10 \end{array} \right\}$$

$$\left\{ \begin{array}{l} P_F(r) = \left(\frac{3\pi^2 \rho(r)}{2} \right)^{1/3} \\ E_F(r) = \hbar^2 \frac{(3\pi^2 \rho(r))^{2/3}}{2m_N} \end{array} \right\}$$

$$\left\{ \begin{array}{l} V \equiv V_N = E_F + \text{Binding energy} \\ V_\pi = 25 \text{ MeV} \end{array} \right\}$$

Quasi free scattering

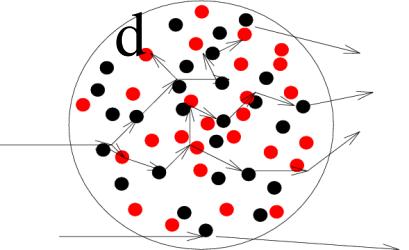
$$\lambda \ll d$$

$$\lambda \ll \Lambda$$

λ =de-Broglie wavelength

d =distance between two nucleon

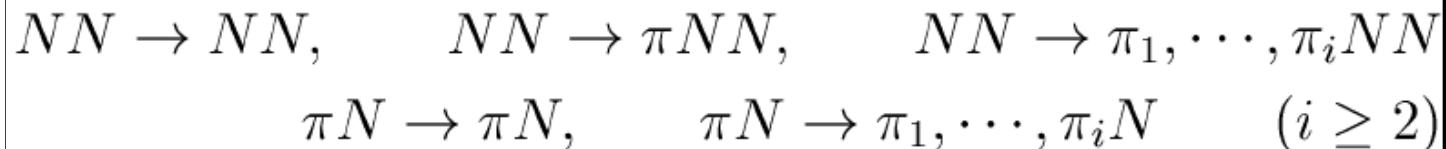
L =mean free path inside nucleus



Drawback of this theory

It is not self consistent theory

It is based on experimental knowledge



Reactions

$$\left\{ \begin{array}{l} \cos(\theta) = 2\xi^{1/2} \left[\sum_{n=0}^N a_n \xi^n + (1 - \sum_{n=0}^N a_n) \xi^{N+1} \right] - 1 \\ a_n = \sum_{k=0}^N a_{nk} E^k \\ N=3, M=3 \end{array} \right\}$$

Angular distribution

Cross-section

$$\left\{ \begin{array}{ll} p + p = p + p & \text{Isotropic } E < 0.46 \text{ GeV} \\ p + p = p + p & 0.46 < E < 2.8 \text{ GeV} \\ p + p = p + p & 2.8 < E < 10.0 \text{ GeV} \\ p + n = p + n & E < 0.97 \text{ GeV} \\ \pi^+ + p = \pi^+ + p & E < 80.0 \text{ MeV} \\ \pi^+ + p = \pi^+ + p & 80 < E < 300.0 \text{ MeV} \\ \pi^+ + p = \pi^+ + p & 0.3 < E < 1.0 \text{ GeV} \\ \pi^+ + p = \pi^+ + p & 1.0 < E < 2.4 \text{ GeV} \end{array} \right\}$$

Pre-equilibrium model (Exciton model)

Cut off energy (7 MeV) is the criteria to close INC

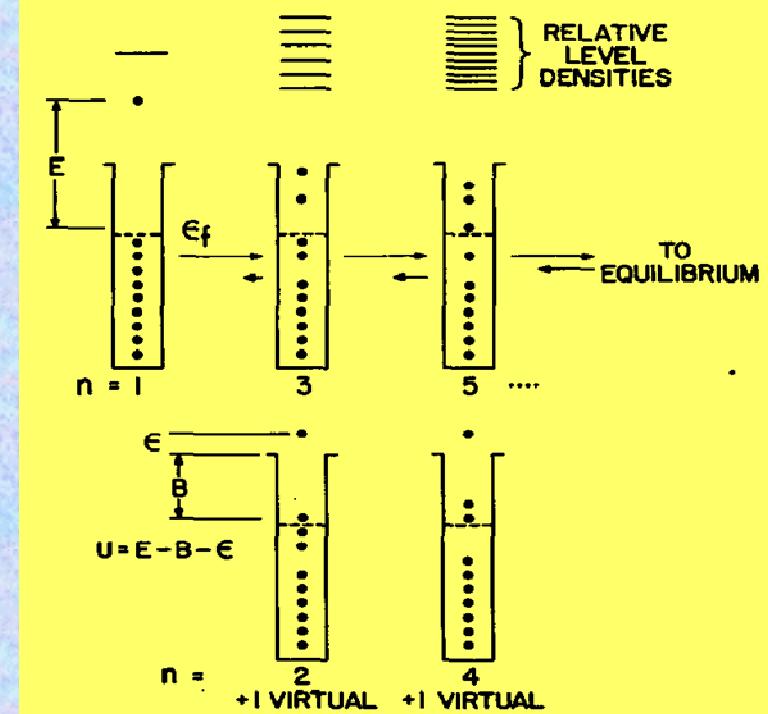
n, p, d, t, ${}^3\text{He}$, and ${}^4\text{He}$ emission

Probability of emission is calculated as given below

$$\begin{aligned}\Gamma_j(p, h, E) &= \int_{V_j^c}^{E - B_j} \lambda_c^j(p, h, E, T) dT , \\ \lambda_c^j(p, h, E, T) &= \frac{2s_j + 1}{\pi^2 \hbar^3} \mu_j \Re_j(p, h) \frac{\omega(p - 1, h, E - B_j - T)}{\omega(p, h, E)} T \sigma_{inv}(T)\end{aligned}$$

p=particle, h=hole, n=p+h is exciton number, s=spin,

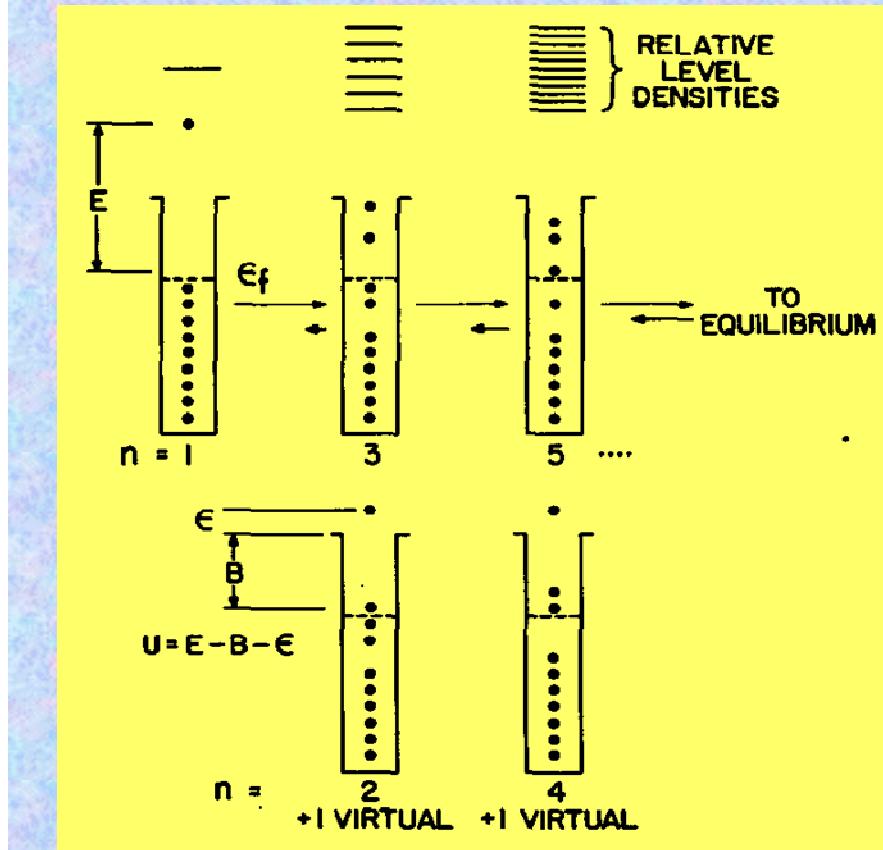
σ_{inv} =cross-section, E=excitation energy, B=binding energy



Normalize p, d, t, ${}^3\text{He}$, and ${}^4\text{He}$ emission probability to 1
 Generate random number
 Select the probable one

Evaporation model

How do we reach equilibrium



$$\lambda_+(n_{eq}, E) = \lambda_-(n_{eq}, E) \quad n_{eq} \simeq \sqrt{2gE}$$

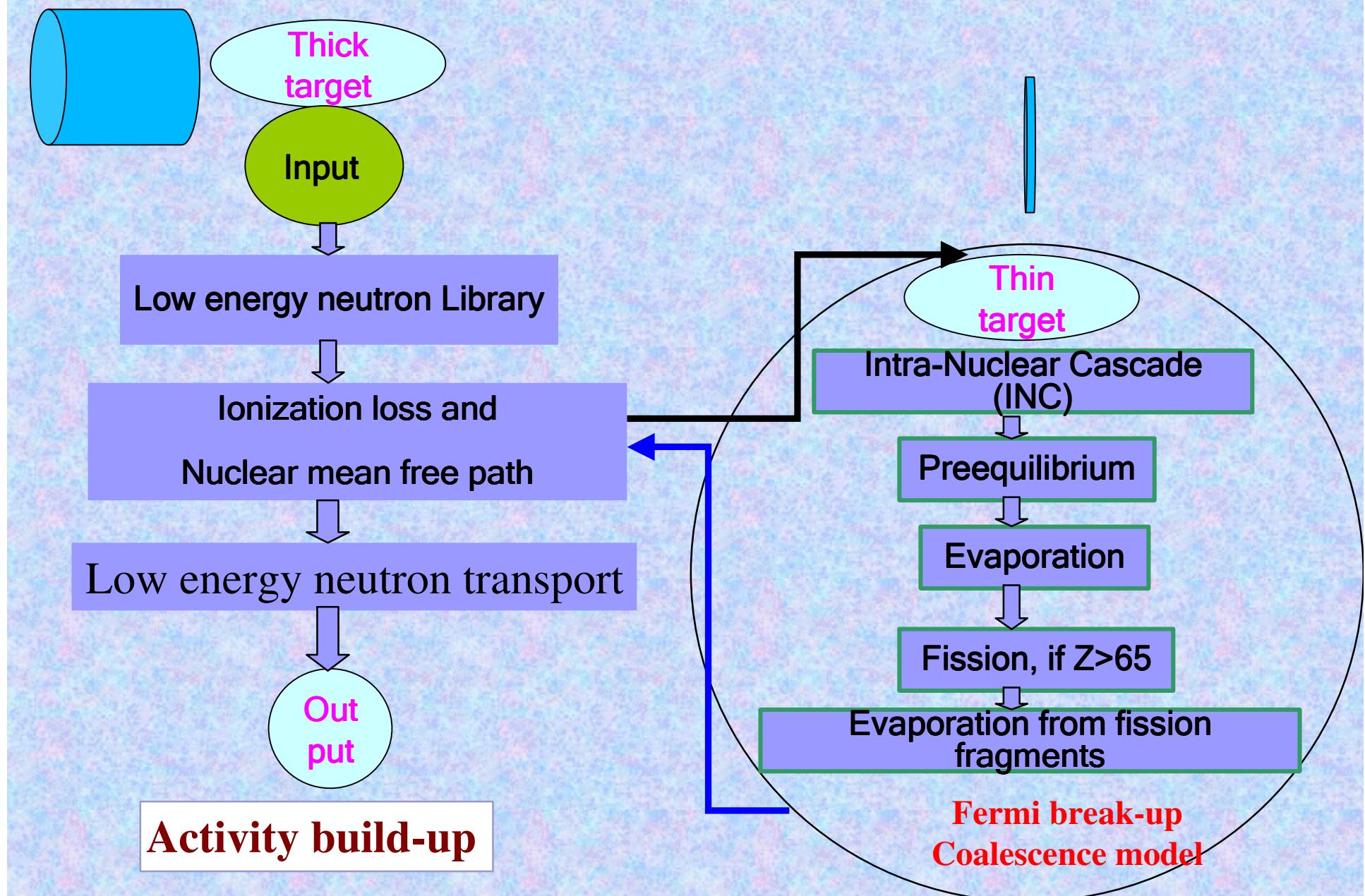
$$P_j(\epsilon)d\epsilon = g_j \sigma_{inv}(\epsilon) \frac{\rho_d(E - Q - \epsilon)}{\rho_i(E)} \epsilon d\epsilon$$

Z_j	Ejectiles						
0	n						
1	p	d	t				
2	^3He	^4He	^6He	^8He			
3	^6Li	^7Li	^8Li	^9Li			
4	^7Be	^9Be	^{10}Be	^{11}Be	^{12}Be		
5	^8B	^{10}B	^{11}B	^{12}B	^{13}B		
6	^{10}C	^{11}C	^{12}C	^{13}C	^{14}C	^{15}C	^{16}C
7	^{12}N	^{13}N	^{14}N	^{15}N	^{16}N	^{17}N	
8	^{14}O	^{15}O	^{16}O	^{17}O	^{18}O	^{19}O	^{20}O
9	^{17}F	^{18}F	^{19}F	^{20}F	^{21}F		
10	^{18}Ne	^{19}Ne	^{20}Ne	^{21}Ne	^{22}Ne	^{23}Ne	^{24}Ne
11	^{21}Na	^{22}Na	^{23}Na	^{24}Na	^{25}Na		
12	^{22}Mg	^{23}Mg	^{24}Mg	^{25}Mg	^{26}Mg	^{27}Mg	^{28}Mg

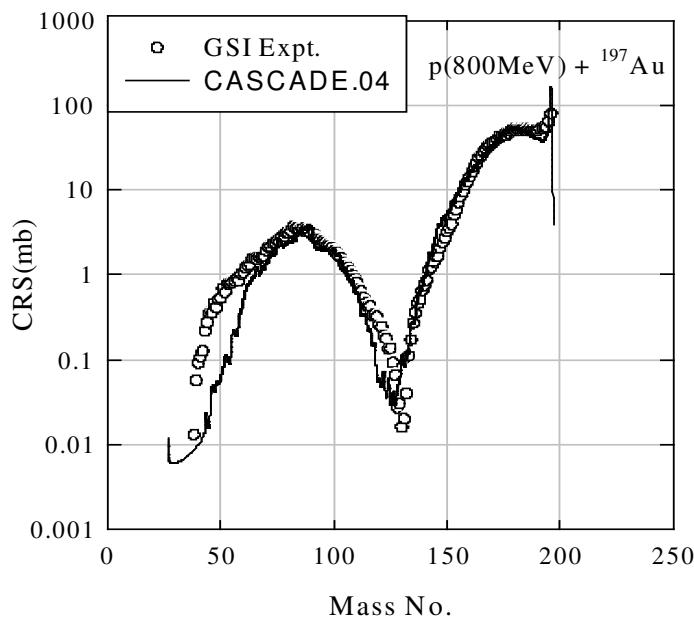
$$\rho(E) = \frac{c_1 \exp(2\sqrt{a(E - \delta)})}{a^{1/4}(E - \delta)^{5/4}}$$

$$a(A_d, Z_d, E) = A_d(0.134 - 1.2110^{-4}A_d)(1 + \frac{S}{E}(1 - \exp(-0.061E)))$$

CASCADE.04 general scheme



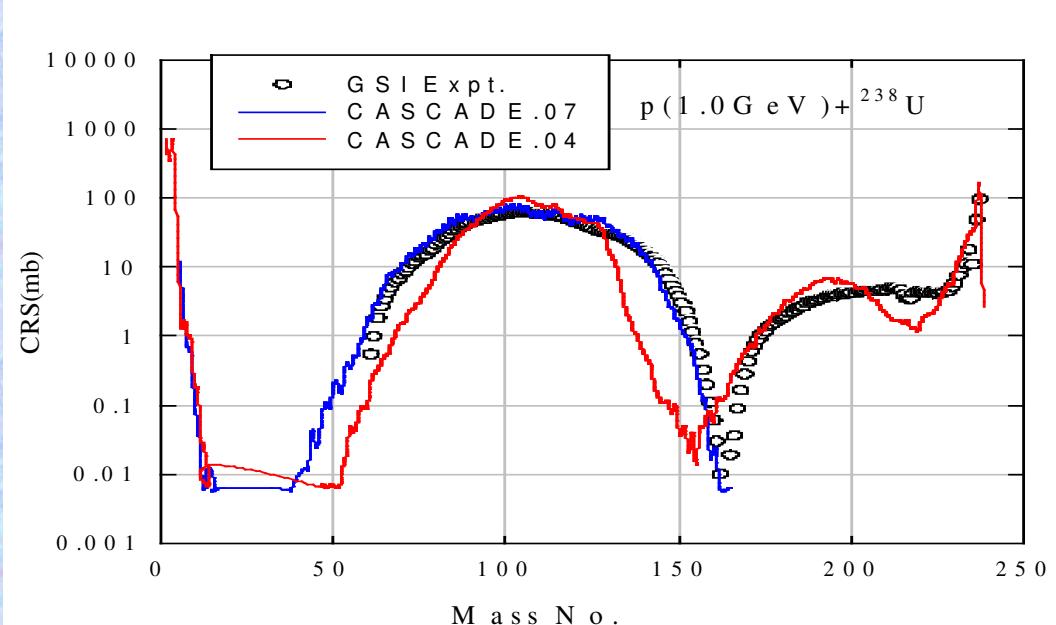
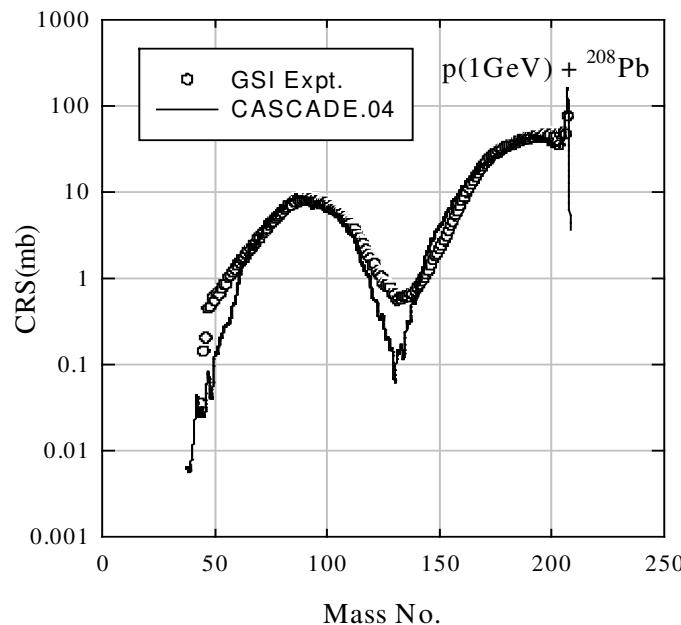
Results, Benchmark



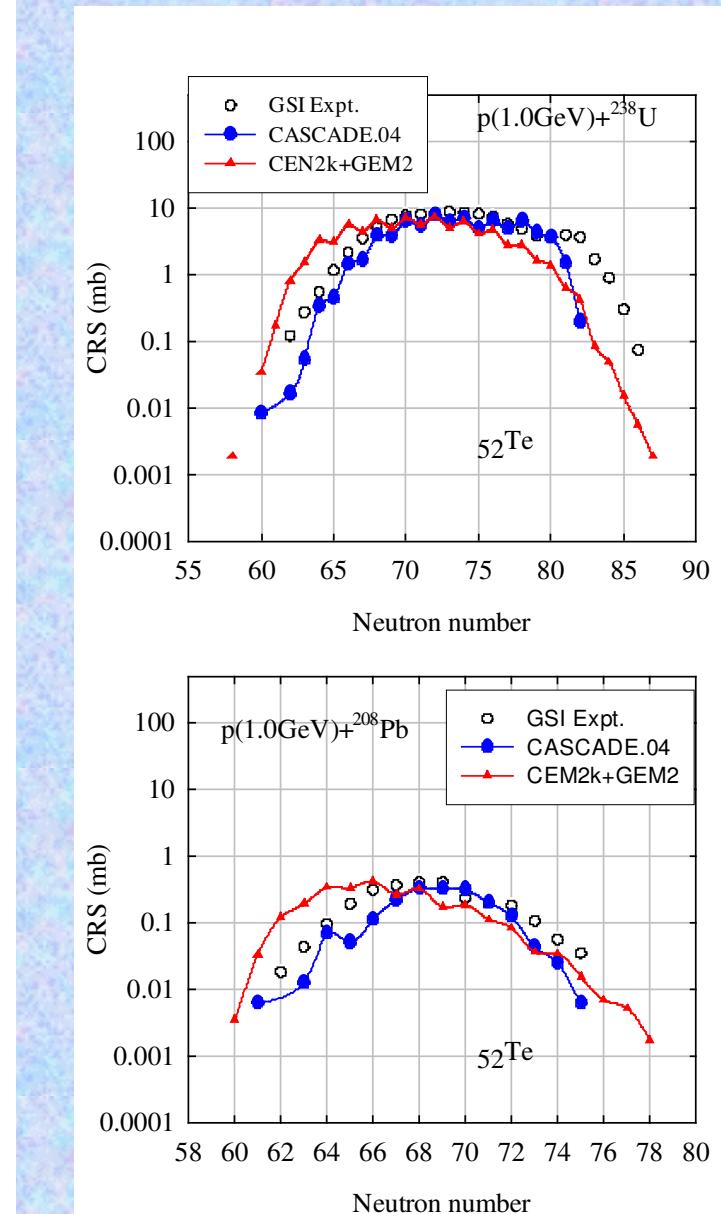
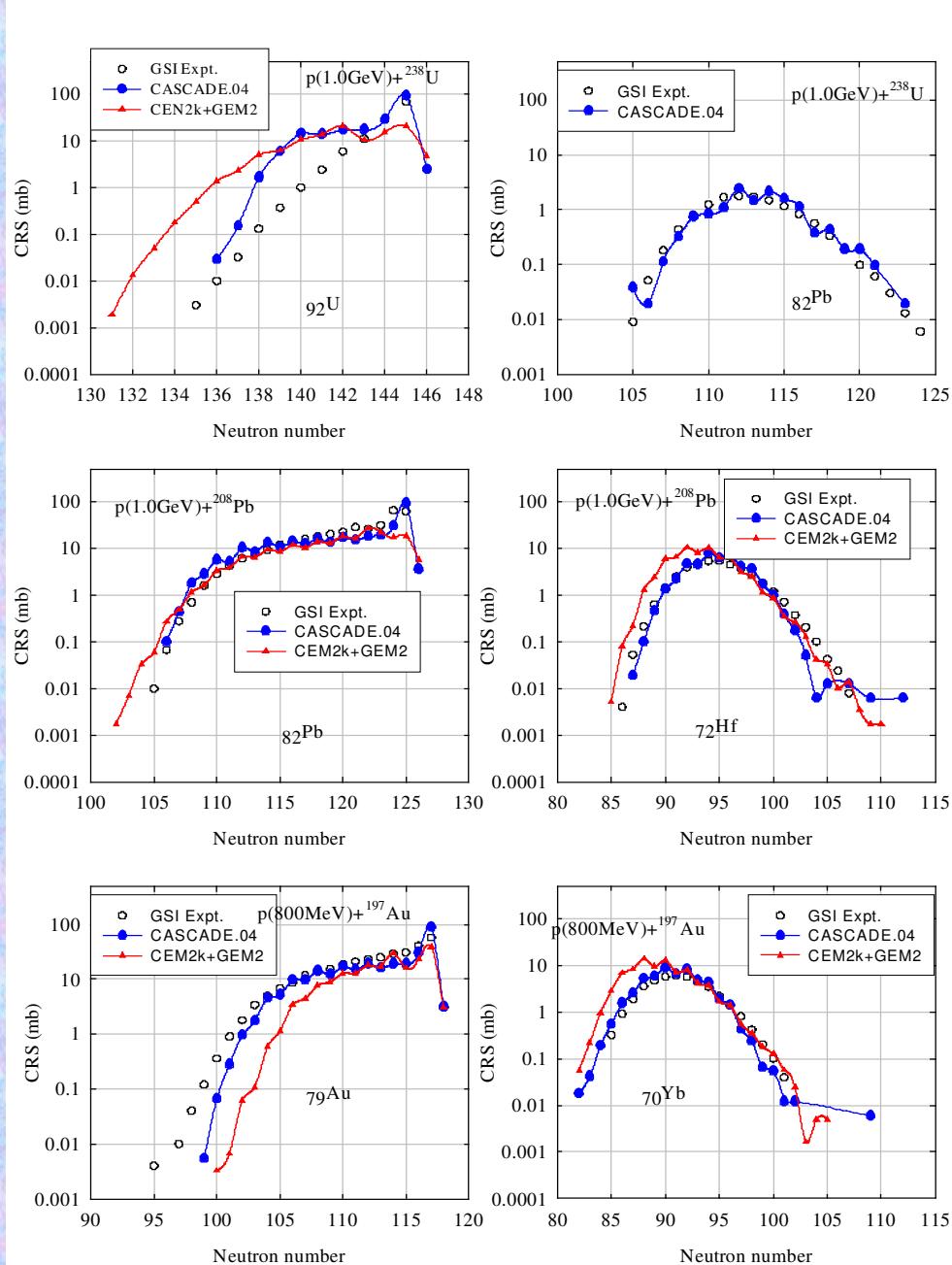
Mass Distributions
Isotope distribution
Excitation function

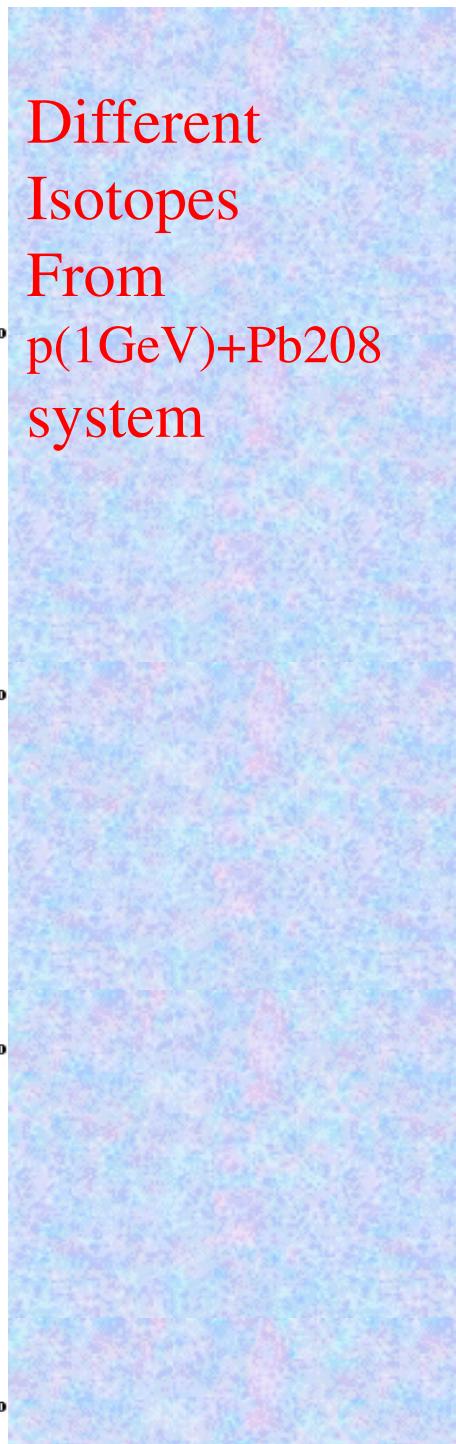
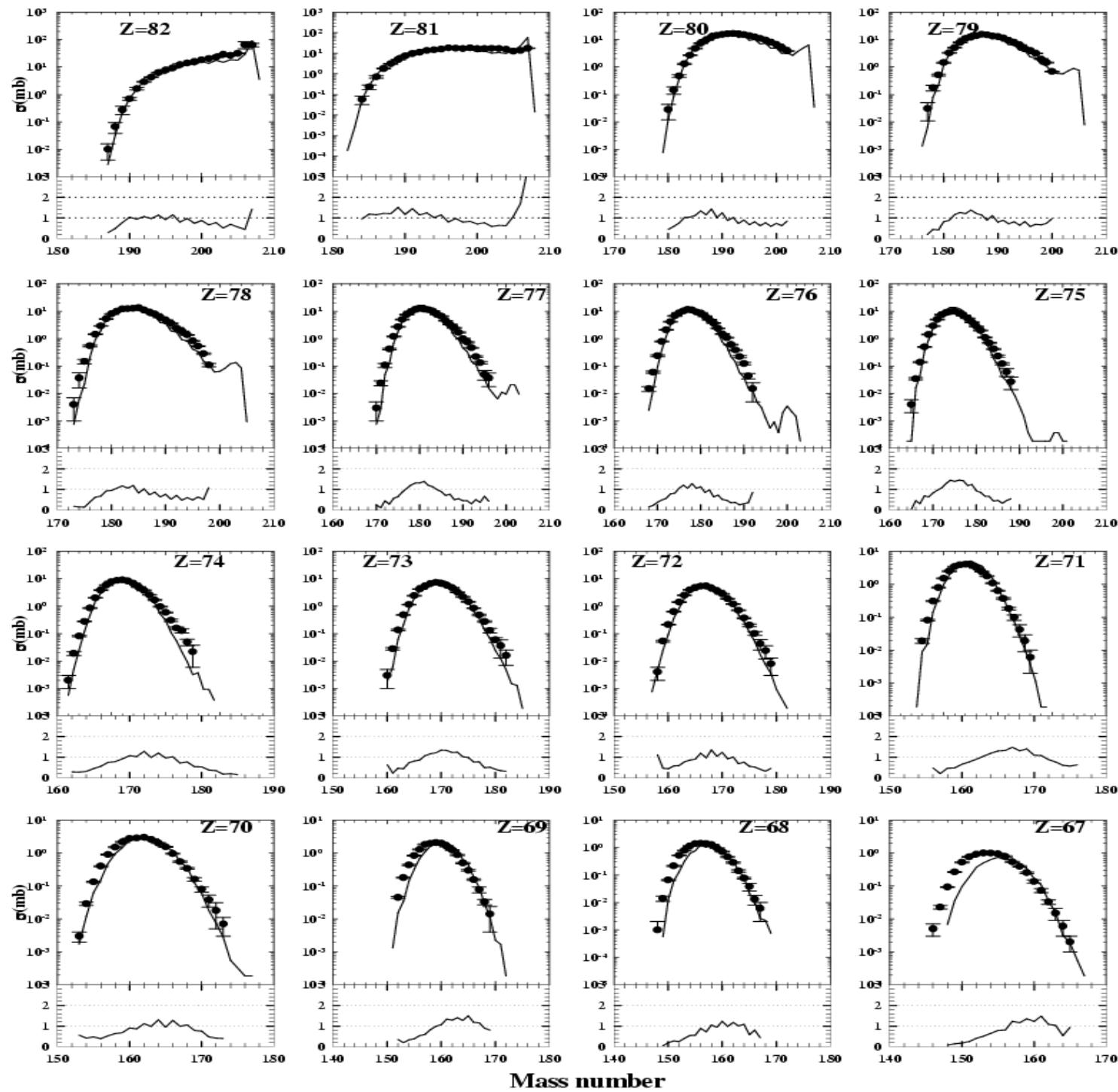
$n, p, d, t, {}^3\text{He}, {}^4\text{He}, p^\square, {}^0$

Thick target simulation



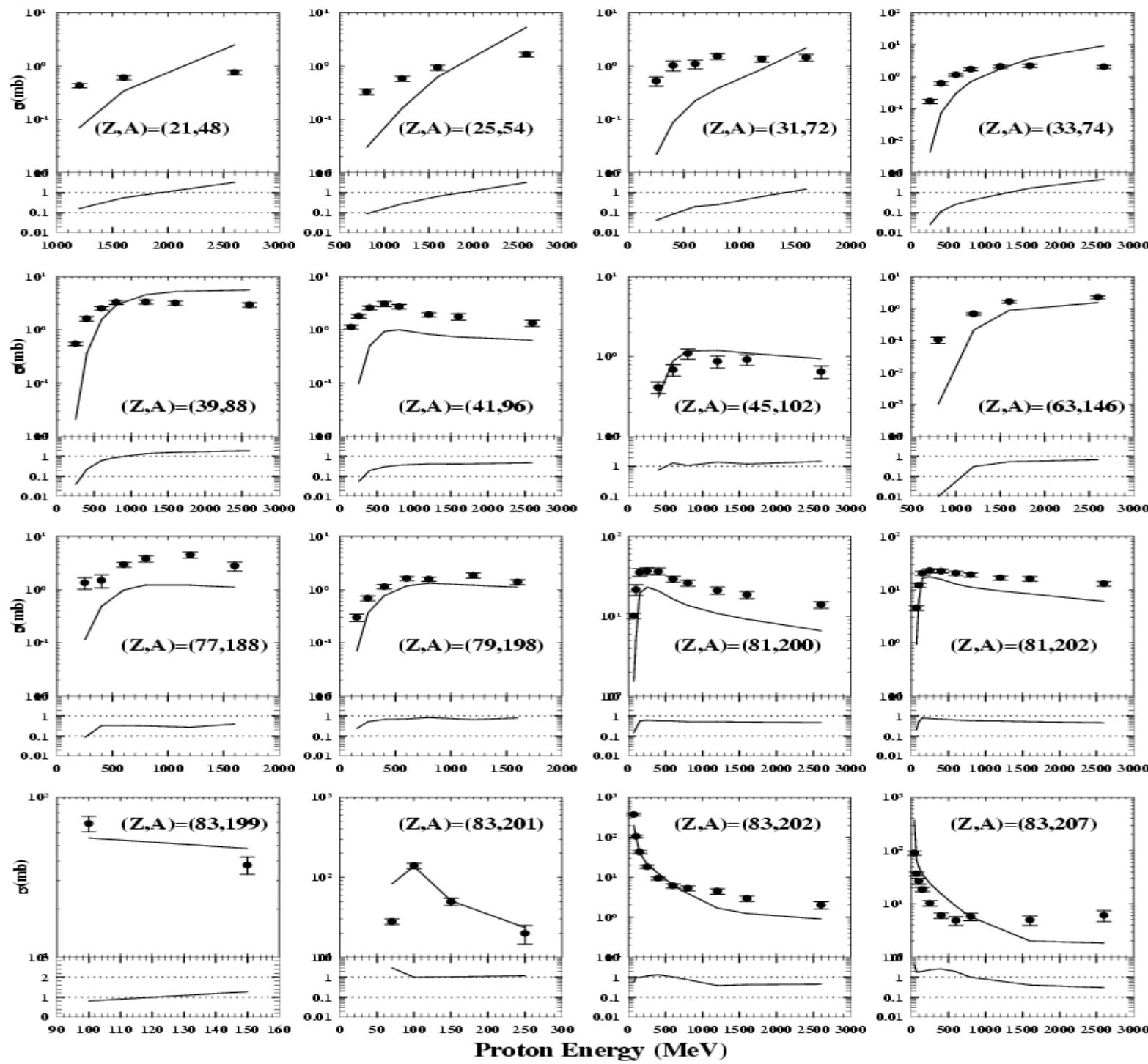
Spallation Evaporation and Fission Residues

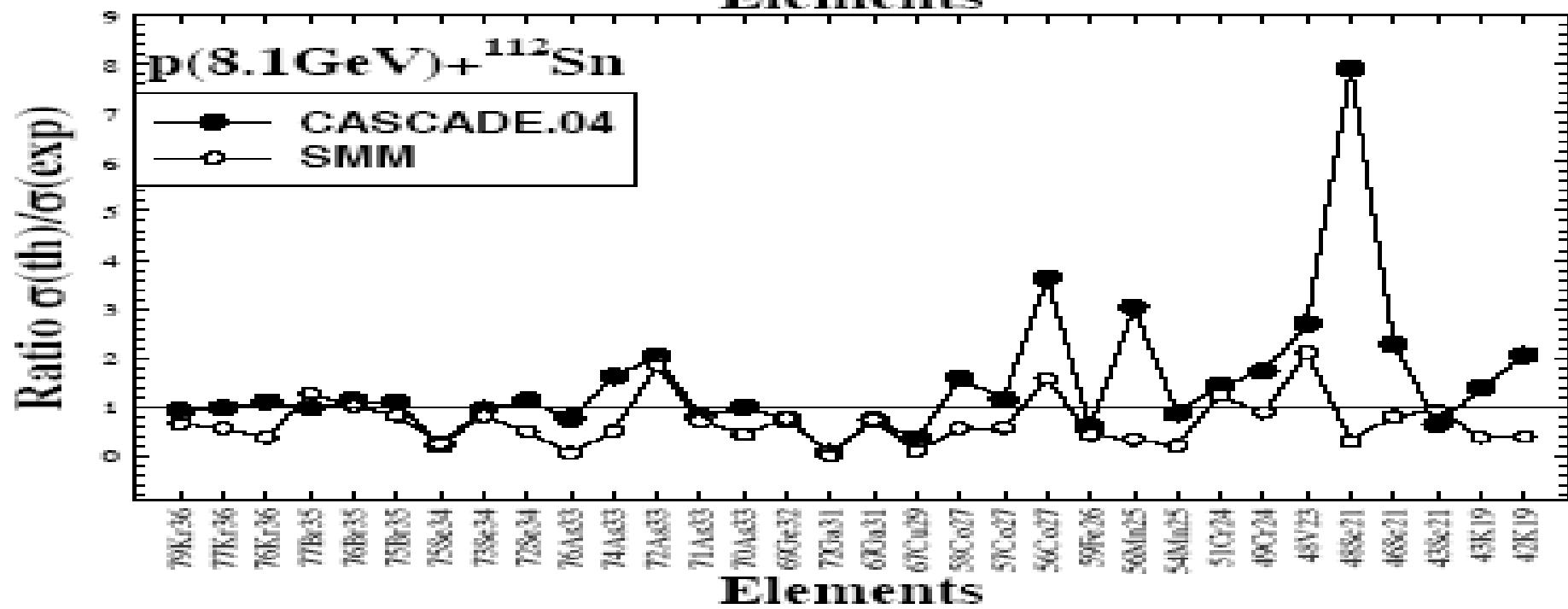
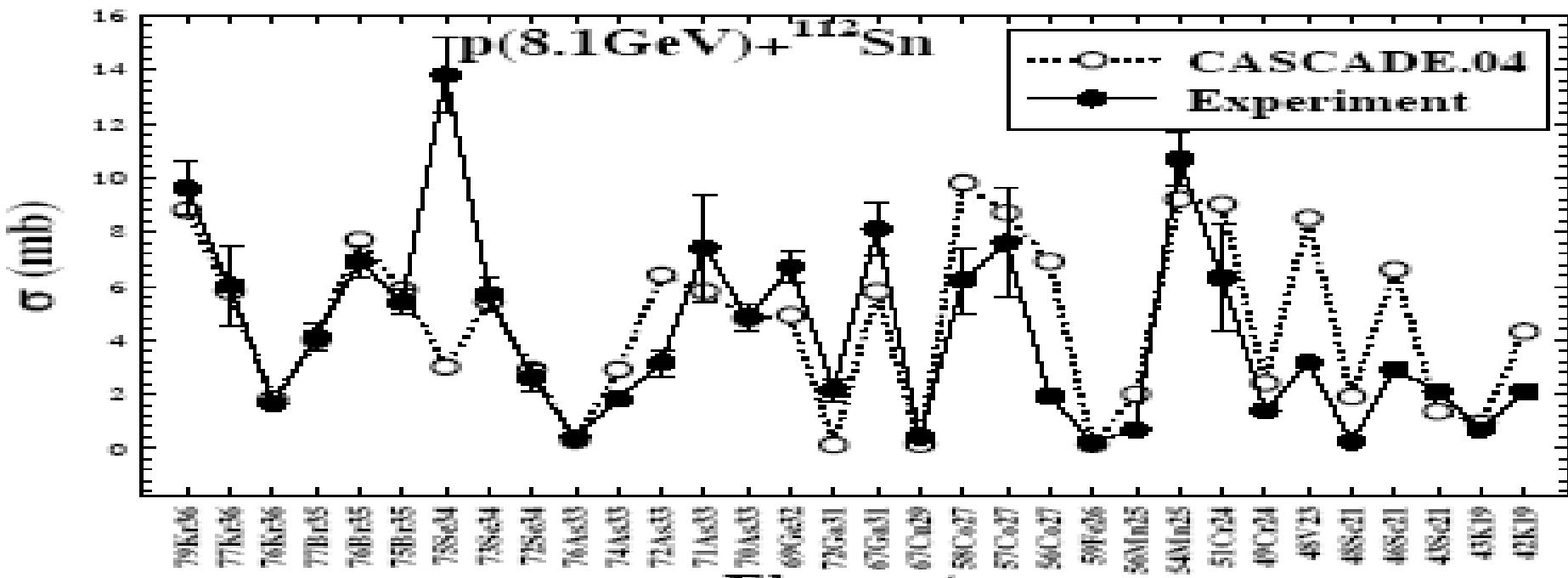


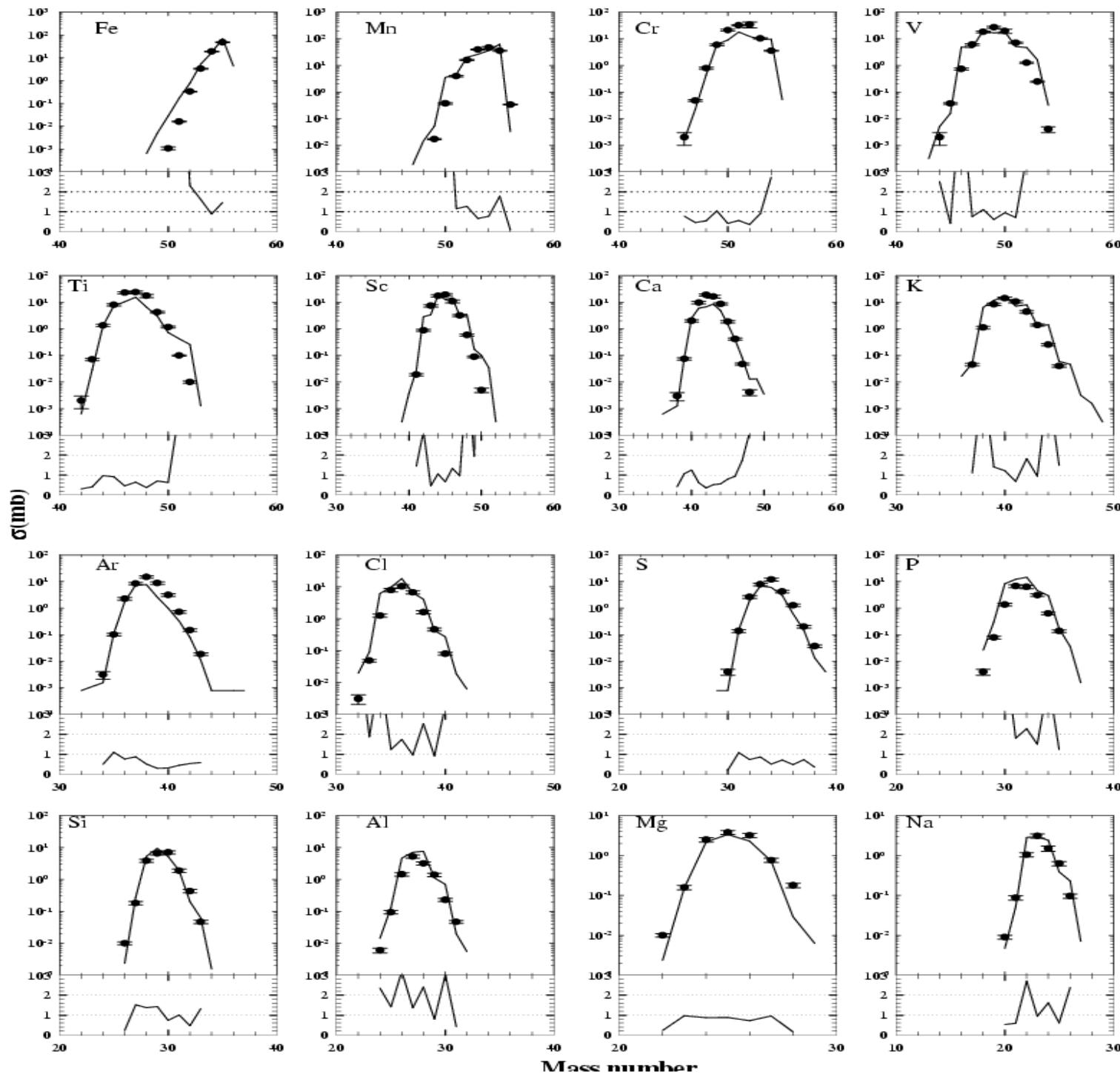


Different Isotopes From $p(1\text{GeV})+\text{Pb}208$ system

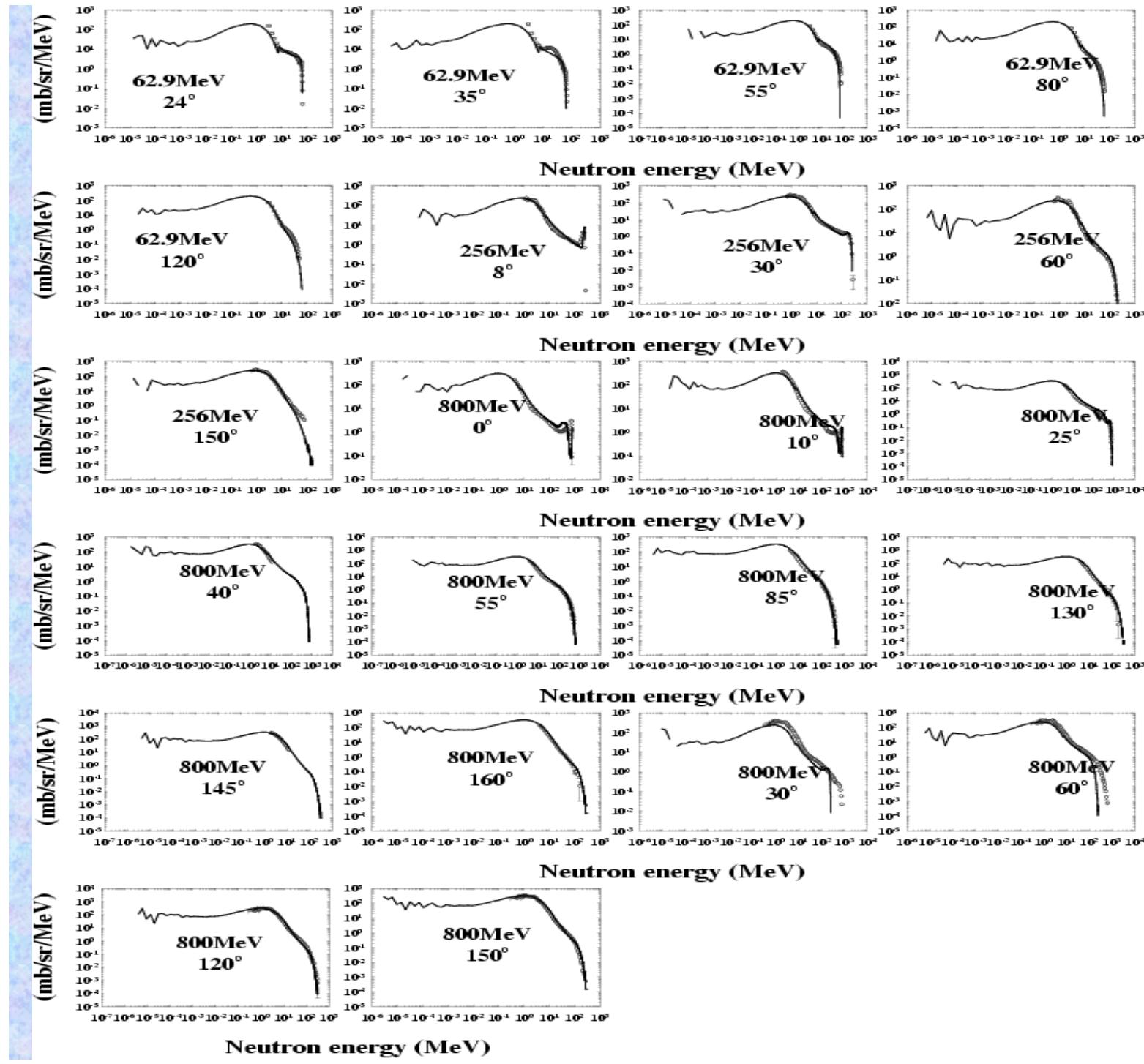
Cross-section For $p+208Pb$





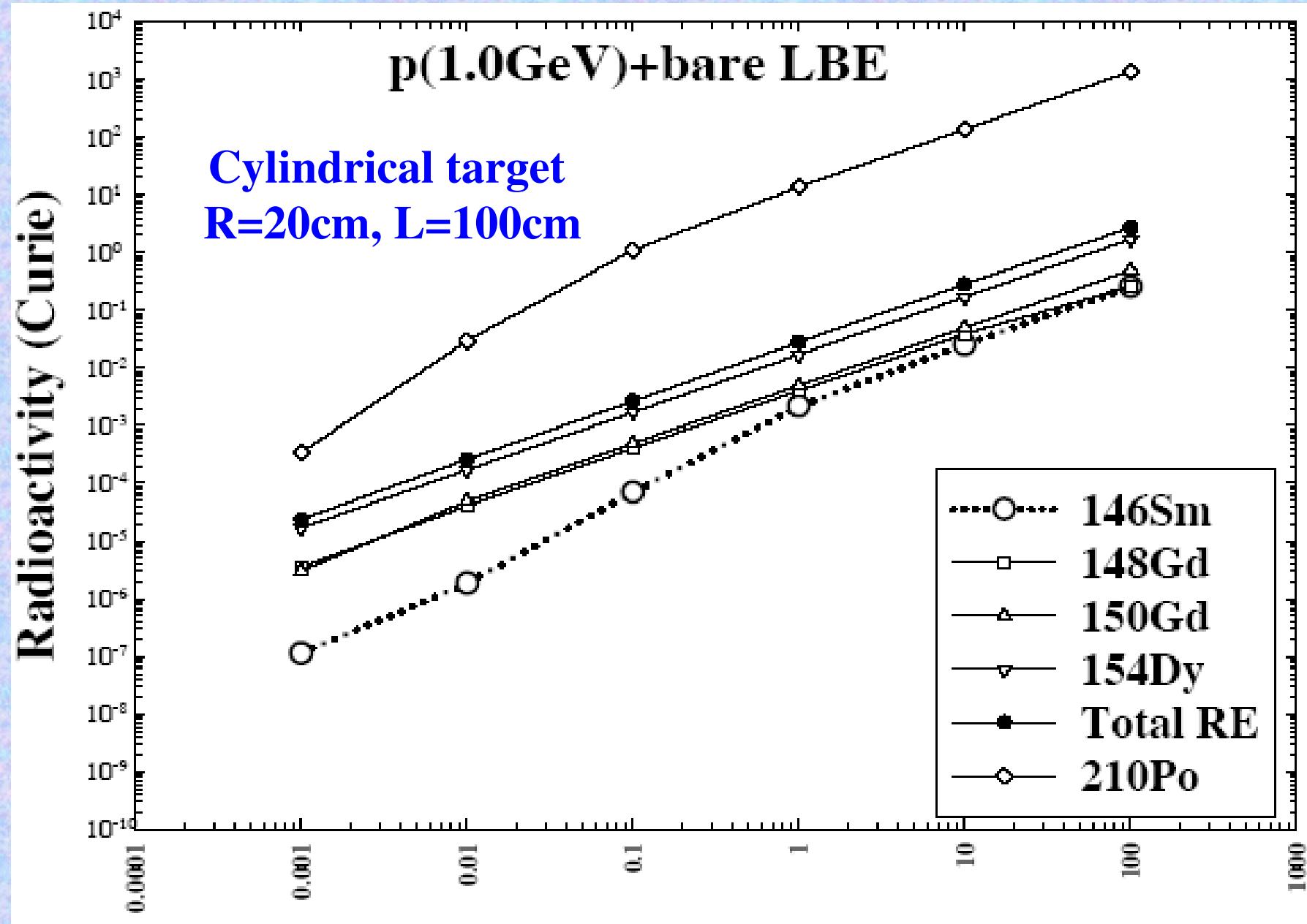


Different Isotopes From $p(1\text{GeV})+\text{Fe}56$ system



Double Differential Neutron Production Cross-section For p+Pb208 system

Alpha radio-activity in LBE due to Rare earth and ^{210}Po



Thick target simulation

Pre-defined geometries:

**Spherical, cylindrical, conical, hexagonal,
elliptical, hemi-sphere, hemi-elliptical, cubic ..**

Low energy data library

26-group data library

**ENDFVII.0 is implemented for Pb²⁰⁸ more to be
done**

**Ionization/Stopping power calculation is
implemented up to 100GeV**

Coupled with burnup code ☺

Thick target simulation Results

Heat deposition due to primary and secondaries

**Neutron yield, Angular /energy spectra, spatial
and radial flux distribution**

Isotope buildup

Burnup, k_{eff} ?

Biasing:

**Weight cutoff, energy cutoff, geometry splitting
and exponential method**