

Particle and Energy Transport in Dedicated ρ^* , β and v^* Scans in JET ELMy H-modes

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Abstract. Studying plasma transport in terms of the non-dimensional parameters (ρ^* , β , v^*) is a natural way to separate important physical transport processes. ρ^* , the ion Larmor radius normalised to the plasma minor radius, separates Bohm/gyro-Bohm transport; β , the ratio of plasma pressure to magnetic pressure separates electrostatic and electromagnetic transport; and v^* , the ion collision rate scaled to the ion bounce frequency, describes the effect of collisionality. With this in mind, scans have been performed on JET (MarkIIIGB-SRP divertor) with one of ρ^* , β , v^* varied whilst the other two remained fixed. Both particle transport, using trace tritium (T) injection, and energy transport have been studied. The ρ^* behaviour of energy and trace T transport is found to be consistent with the essentially gyro-Bohm like dependence of the scaling used in the ITER design, IPB98(y,2), although trace T confinement in the outer region ($x=0.65-0.85$) is Bohm like ($D/B_0 \propto \rho^{*-1.90 \pm 0.38}$). The v^* scans showed energy confinement decreasing with increasing v^* ($B_0 \tau_E \propto v^{*-0.35 \pm 0.04}$) more strongly than in IPB98(y,2), with trace T confinement having the opposite trend although the results are more ambiguous. The three β scans show a negligible effect of β on energy confinement ($B_0 \tau_E \propto \beta^{*0.04}$, $\beta^{*-0.03}$, $\beta^{*-0.01}$), in contrast to IPB98(y,2), which is consistent with electrostatic models. Trace T confinement, however, increases with increasing β ($D \propto D_{g-Bohm} \beta^{*-0.34 \pm 0.08}$, $D \propto D_{Bohm} \beta^{*-0.55 \pm 0.09}$) which is inconsistent with IPB98(y,2) and electrostatic models, but is shown to be consistent with a model based on stochastic electromagnetic fields. It remains to describe both particle and energy transport with a unified model. Extrapolation of these results to ITER indicates a moderate increase in energy confinement time for $\beta_N=1.8$ (2%), but a dramatic improvement for higher β_N (e.g. 50% higher for $\beta_N=3$). The impact on ITER of increased particle confinement at high β_N remains to be assessed.

1. Introduction

In the ITER design [1], energy and particle confinement are based upon IPB98(y,2) scalings,

$$\tau_E = \tau_{IPB98(y,2)} = 5.62 \times 10^{-2} \cdot P_{loss}^{-0.69} B_0^{0.15} I_p^{0.93} \kappa_a^{0.78} \bar{n}_e^{0.41} a^{0.58} R^{1.39} M^{0.19} \quad (1a)$$

$$\tau_{p,He} = 5 \times \tau_{IPB98(y,2)}, \quad (1b)$$

which have been derived from a wide database (DB3v5) of multi-machine confinement experiments [2] and, in the case of energy confinement, are consistent with experimental measures over almost 3 orders of magnitude. The IPB98(y,2) scaling has been shown to be consistent with the Kadomtsev [3] constraint, and so may be cast in the dimensionless form

$$B_0 \tau_{IPB98(y,2)} \propto \rho^{*-2.70} \beta^{-0.90} v^{*-0.01} M^{0.96} q_{95}^{-3.0} \varepsilon^{0.73} \kappa^{3.3}. \quad (2)$$

¹ See appendix of paper by J. Pamela *et al.*, *this conference*

However, as IPB98(y,2) is derived on largely empirical grounds from a single regression to a database known to have correlated regressors and non-random error sources, several alternative and independent estimates of plasma confinement scaling have also been attempted. One such method is that of dimensionless variable scans, which enables the dependence of confinement on individual dimensionless physics parameter to be studied (it should be noted that particle and energy confinement times and diffusivities are normalised as $\omega_{ci}\tau_E \propto B_0\tau_E$, $\chi/\omega_{ci}a^2 \propto \chi/B_0$, $D/\omega_{ci}a^2 \propto D/B_0$ [3]). This method has the additional advantage that the dimensionless parameters (ρ^* , β , v^*) have been chosen so as to naturally separate various transport models with, for example, $B_0\tau$ proportional to ρ^{*-2} (ρ^{*-3}) for Bohm like (gyro-Bohm like) transport, and $B_0\tau$ independent (dependent) on β for electrostatic (electromagnetic) transport. ρ^* , β , and v^* are local parameters, but in the rest of this paper they will be used to refer strictly to their global, volume averaged, values.

Dimensionless variable scans on a single machine involve a series of discharges at different fields. In each type of scan, one dimensionless variable varies whilst the rest are fixed. This implies that plasma current, density and temperature must all vary as a certain function of the field (Table I). Experimentally, this is achieved through the direct selection of plasma current and the tuning of gas fuelling and input power until variables are matched within their measurement errors (taken for JET as 2.7% for ρ^* , 6.0% for β , 10.4% for v^* , and 8.3% for $B\tau_E$ [4]). A bulk ion particle transport ρ^* scan experiment has been performed previously at JET [5], indicating a mixture of Bohm and gyro-Bohm transport, but the other parameters were not well matched. Dimensionless parameter scan studies of energy transport have been performed on several machines, including JET [6], but the ones presented here are more extensive.

TABLE I: SCALING OF VARIABLES IN DIMENSIONLESS PARAMETER SCANS

Scanned parameter	Fixed parameters	Scalings
$\rho^* \propto T^{1/2}/B_0$	β , v^* , q_{95}	$I \propto B_0$, $n \propto B_0^{4/3}$, $T \propto B_0^{2/3}$
$\beta \propto nT/B_0^2$	ρ^* , v^* , q_{95}	$I \propto B_0$, $n \propto B_0^4$, $T \propto B_0^2$
$v^* \propto n/T^2$	ρ^* , β , q_{95}	$I \propto B_0$, $n \propto B_0^0$, $T \propto B_0^2$

2. Particle Transport Experiments with Trace Tritium

TABLE II: DISCHARGES FOR TRACE TRITIUM ELMY H-MODE (ρ^* , β , v^*) SCANS

Pulse	time [s]	I_p [MA]	ρ^*/ρ^*_{ITER}	β_N	v^*/v^*_{ITER}	D_{inner}/B_0 [m ² s ⁻¹ T ⁻¹]	D_{outer}/B_0 [m ² s ⁻¹ T ⁻¹]
61103	14.0	2.75	2.46	1.68	1.90	0.137	0.277
61174	22.0	2.35	2.84	1.89	2.03	0.280	0.364
61097	23.0	2.00	3.14	1.88	2.34	0.291	0.440
61132	23.0	2.35	2.77	0.58	1.53	0.137	0.393
61530	22.0	2.00	2.88	1.94	3.63	0.151	0.260

Bulk particle transport has been studied by monitoring the propagation of trace tritium (T) using 14 MeV neutron cameras with 10 horizontal and 9 vertical channels (see [7] for a fuller discussion). To provide the dimensionless variable scans, ELMY H-mode discharges, at low q ($q_{95}=2.8$) and triangularity ($\delta=0.2$), were prepared in pure deuterium plasmas as outlined in section 1. In each case, these were then repeated with a trace T gas puff (2.5-5 mg over

80ms). In all but one case (the mid- ρ^* point), a matched discharge was also performed with T seeding from a 100keV NBI source (1.2MW for 100ms) to separate out wall fuelling effects. The resulting discharges (Table II) provided a three-point ρ^* scan (#61103, #61174, #61097),

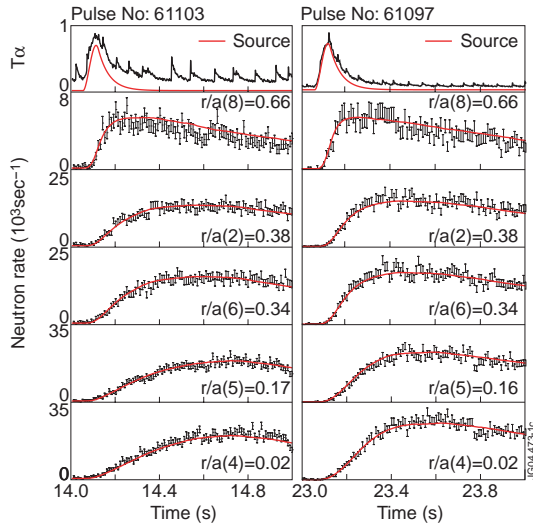


FIG. 1. Evolution of the edge T_α (top) and D-T neutron emission, viewed on five different chords (below), following an 80ms T puff, for two Type I ELMy H-Mode shots. Data is shown in black and the prediction from the fitted transport coefficients in pink and red.

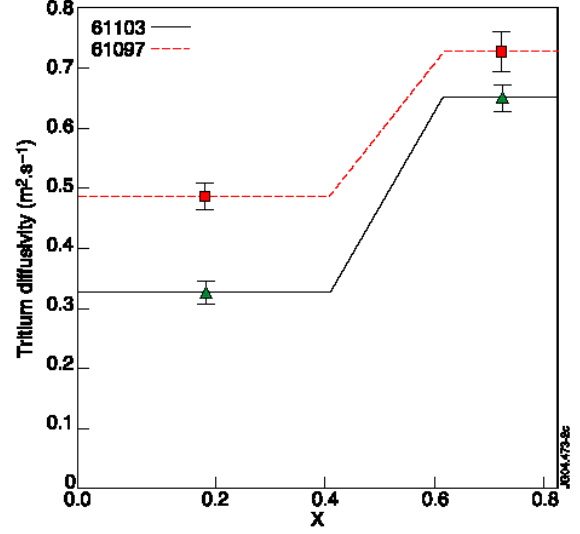


FIG. 2. The T diffusivity profiles for the fits shown in FIG. 1.

a two-point β scan (#61103, #61132), and a two-point v^* scan (#61174, #61530). The low β discharge in the β scan is a Type III ELMy H-mode and problems of access to the Type III regime led to the relatively poor match in ρ^* and v^* .

Particle transport of the tritons is described by an advection, v , and diffusion, D , model

$$\frac{\partial n_T}{\partial t} = \nabla \cdot (n_T v - D \nabla n_T) + s. \quad (3)$$

The edge source was measured by visible spectroscopy and the source profile, s , was calculated from it using a neutral particle model. Assuming v and D to be functions of the bulk species, they can be taken as constant in time. They are then parameterised (3 parameters for D and 3 for v) and the T density profile as a function of time is forward modelled and the 14MeV neutron data resulting from it calculated. D and v are then varied until the closest least squares fit to the neutron data is found. This is performed by the UTC code with the transport modelling performed by the 1½-D impurity transport model SANCO and the resulting 14 MeV neutrons calculated by a method based on the TRANSP code (see [7] for a fuller discussion). This paper will concentrate on the diffusion coefficient, which is parameterised to have constant values in the regions $x=0-0.45$, $x=0.65-0.85$ and $x=0.86-1.0$, and to be linearly connected in between (x is defined as the square root of the toroidal flux normalised to its value at the separatrix). FIG. 1 shows the resulting fits to two discharges (#61097 and #61103) and FIG. 2 the calculated diffusion profile for discharge #61097. Transport will be studied in the inner ($x=0-0.45$) and outer ($x=0.65-0.85$) regions, as the region from $x=0.85-1.0$ is assumed to be affected by ELMs.

The two discharges in FIG. 1 represent the high and low points in the ρ^* scan and it can be seen that the time for the T puff to penetrate to the core in the high ρ^* discharge (#61097) is

considerably shorter than that for the low ρ^* (#61103) discharge. This can be interpreted as an increase in diffusivity (FIG. 3), D_T , with increasing ρ^* . A log-linear regression to the inner and outer diffusion measures gives the scalings

$$D_{inner}/B_0 \propto \rho^{*3.22 \pm 0.62}, \quad D_{outer}/B_0 \propto \rho^{*1.90 \pm 0.38}. \quad (4)$$

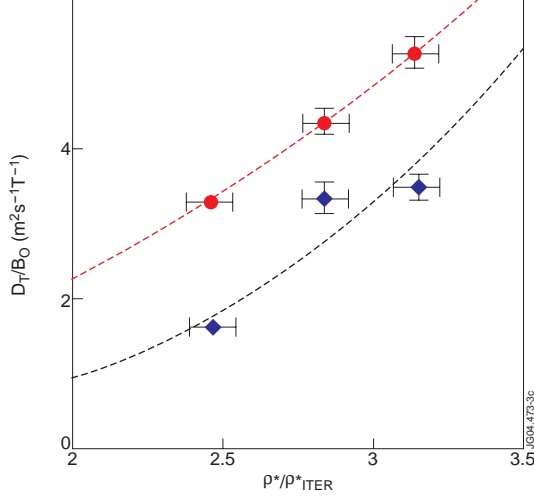


FIG. 3. Normalised T diffusivity, against ρ^* , normalised to ITER, for the inner ($x=0-0.45$; blue diamonds) and outer ($x=0.65-0.85$; red circles) regions for shots #61103, #61174, and #61097 (Table 1). The fits of equation 4 are shown as broken lines.

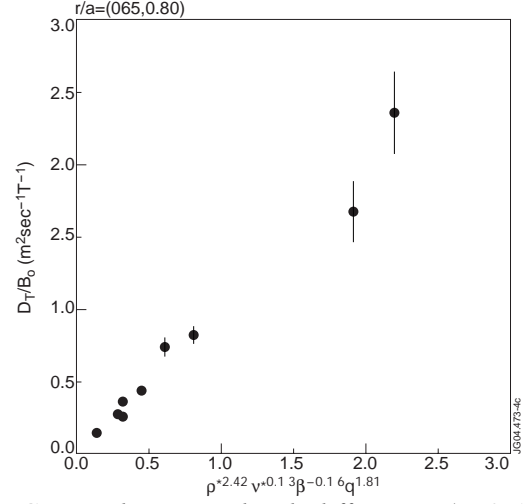


FIG. 4. The normalised diffusivity ($x=0.65-0.85$), measured by trace T gas puffing, for 12 ELMy H-modes, against a log-linear regression to the variables (ρ^*, β, v^*, q) (6)

A strong, gyro-Bohm like, dependence is seen in the inner region and a weaker, Bohm like, dependence in the outer region, both with relatively large standard deviations. Proceeding in a similar vein for the β and v^* scans, gives

$$D_{inner} \propto D_{g-Bohm} \beta^{-0.34 \pm 0.08}, \quad D_{outer} \propto D_{Bohm} \beta^{-0.55 \pm 0.09}, \quad (5)$$

$$D_{inner}/B_0 \propto v^{*-0.51 \pm 0.17}, \quad D_{outer}/B_0 \propto v^{*-0.40 \pm 0.15},$$

where, as the match for ρ^* in the β scan is relatively poor, the ρ^* dependence has been normalised for using the observed gyro-Bohm like and Bohm like scalings.

To test the robustness of the scalings, a further 4 trace T NBI heated ELMy H-mode discharges, with varying configurations and q -profile, were added to the dedicated scans to produce a database of 9 discharges. A log-linear regression of the parameters (ρ^*, β, v^*, q) to the normalised diffusivity in the region $x=0.65-0.85$ for this database (FIG. 4) gives

$$D_{ELMy}/B_0 \propto \rho^{*2.4} \beta^{-1.08} v^{*-0.13} q^{1.81}. \quad (6)$$

As with the dedicated scans, trace T confinement is between Bohm like and gyro-Bohm like, increasing strongly with increasing β and weakly with increasing v^* . In contrast to (1b), the correlation between thermal and trace T diffusivity in the 9 discharges is weak ($D/\chi=0.3-1.5$).

3. Energy Transport Experiments

For the energy transport experiments a ν^* scan was performed [8] in a high triangularity, high q scenario ($q_{95} = 4.4$, $\delta \sim 0.4$, $\kappa = 1.7$, $a = 0.92\text{m}$, $R = 2.9\text{m}$). Plasma current was varied from 0.68-1.17 MA, and B_0 varied from 0.96-1.6T. A set of 4 shots was produced (FIG. 5) with a log-linear regression giving an energy confinement scaling of $B_0\tau_E \propto \nu^{*-0.35 \pm 0.04}$ (RMSE=6%).

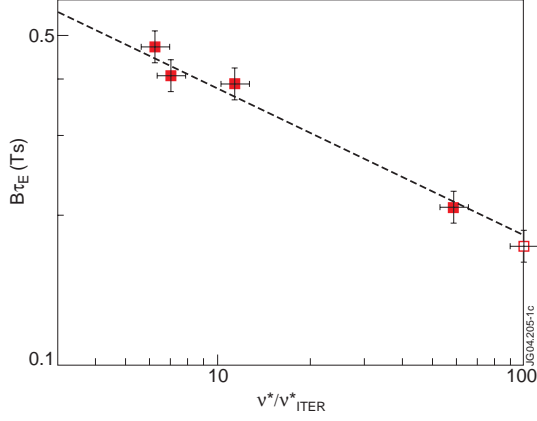


FIG. 5. The normalised confinement time versus the dimensionless collisionality ν^* normalised to that in ITER. The best fit (dashed line) is $B\tau_E \propto \nu^{*-0.35}$

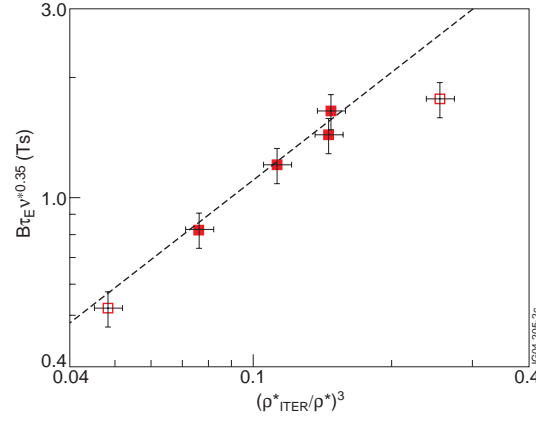


FIG. 6. The normalised confinement time multiplied by $\nu^{*0.35}$ versus the inverse dimensionless Larmor radius cubed normalised to ITER, for type III ELMy H-modes. The best fit is $B\tau_E \nu^{*0.35} \propto \rho^{*-2.9}$.

The ρ^* scans were performed, in the scenario described in section 2, for both Type I ($\beta_t=2.6\%$, $I_p=2\text{-}4\text{MA}$) and Type III ($\beta_t=1.3\%$, $I_p=1.3\text{-}4.3\text{MA}$) ELMy H-modes [8]. For the Type III ELMy H-mode scan (FIG. 6), a log-linear regression gives an energy confinement scaling of $B_0\tau_E \propto \rho^{*-2.9 \pm 0.5}$. The Type I ELMy H-mode scan was affected by variations in the power deposition profile. The relatively low NBI penetration for the low ρ^* (high density) discharges meant that heating profiles varied considerably across the scan (FIG. 7). The resulting ion temperature profiles also varied in broadness (FIG. 8), indicating non-stiff profiles in the parameter range explored. The discharges are thus analysed in terms of their local transport. FIG. 9 shows the variation in effective thermal diffusivity, $\chi = (n_e \chi_e + n_i \chi_i)/(n_e + n_i)$ with ρ^* . A log-linear regression gives $\chi/B_0 \propto \rho^{*3.2 \pm 0.4}$.

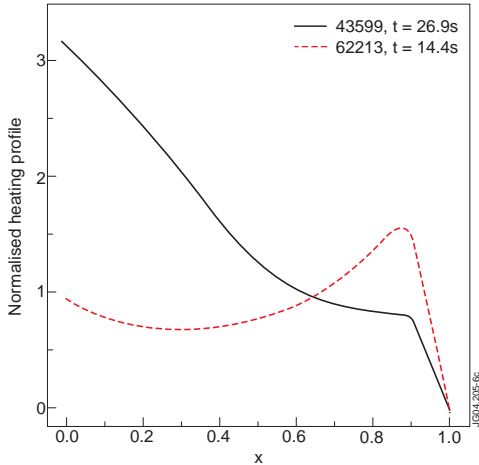


FIG. 7. The heating profiles for the low current (1.46MA) pulse 43599 and the high current (4MA) pulse 62213.

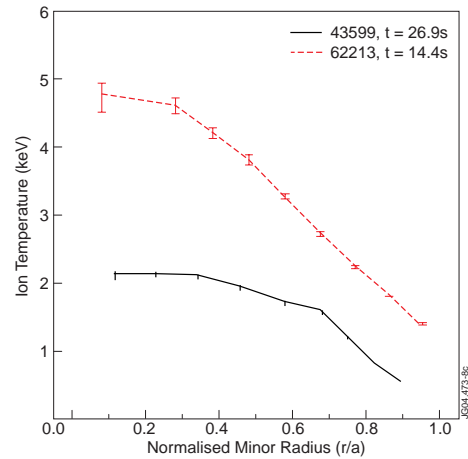


FIG. 8: Ion temperature profiles for the discharges of FIG. 7

Two, two-point β scans were also performed, in the same scenario as section 2, along with a three-point β scan in a higher q ($q_{95}=3.2$) and triangularity ($\delta=0.3$) scenario [4]. In contrast to the IPB98(y,2) scaling, only a very weak β dependence is found ($B_0\tau_E \propto \beta^{*0.04}$, $\beta^{*-0.03}$, $\beta^{*-0.01}$

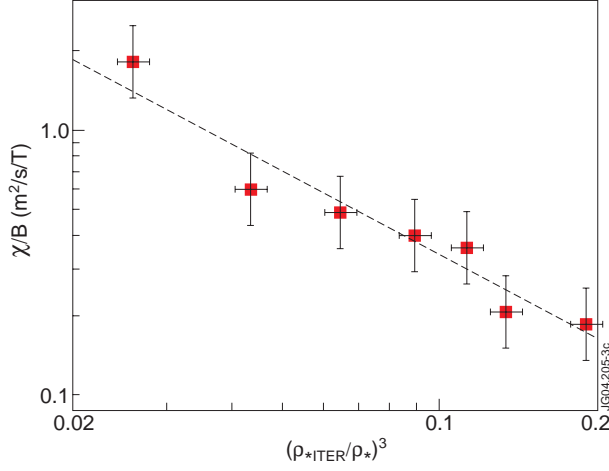


FIG. 9. The dimensionless thermal diffusivity χ/B_0 at $x=0.5$ versus the inverse global dimensionless Larmor radius cubed normalised to the ITER value. The best fit (dashed line) is $\chi/B_0 \propto \rho^{*3.2}$.

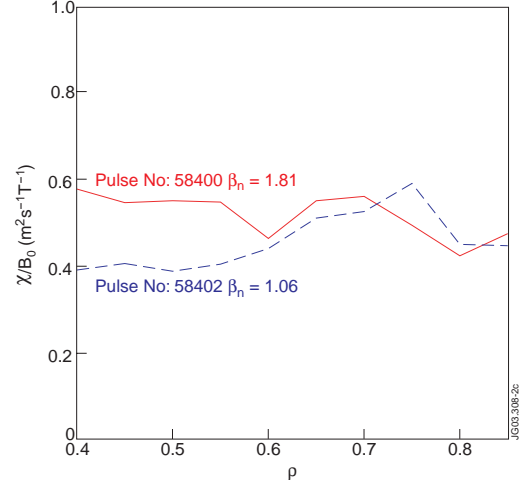


FIG. 10. Radial profiles of the effective thermal diffusivity for two ELMy H-mode discharges with matched ρ^* , v^* , q_{95} , shape and divertor configuration

respectively), consistent with transport dominated by electrostatic processes and in agreement with previous dedicated scans [6, 9]. The three-point scan indicates that this effect is not due to a correlation between β and ELM Type. An analysis of the local transport, using the TRANSP code, shows a similar weak dependence of the effective thermal diffusivity across the plasma (FIG. 10). Similar results have been observed in DIII-D [10].

4. Discussion

TABLE III: SUMMARY OF EXPONENTS OF SCALINGS FOR THE (ρ^* , β , v^*) SCANS

	IPB98(y,2) $B_0\tau_E$	Energy		Trace T	
		$B_0\tau_E$	χ/B_0	D/B_0	
			$x=0.5$	$x=0-0.4$	$x=0.65-0.85$
ρ^*	-2.7	-2.9 ± 0.5	3.2 ± 0.4	3.22 ± 0.62	1.90 ± 0.38
β	-0.9	0.04 ± 0.22 , -0.03 ± 0.16 , -0.01 ± 0.11 (3 scans)		-0.34 ± 0.08	-0.55 ± 0.09
v^*	-2.7	-0.35 ± 0.04		-0.51 ± 0.17	-0.40 ± 0.15

The exponents on (ρ^* , β , v^*) derived from the experiments of sections 2 and 3 are summarised in Table III. The ρ^* scans show that both trace T and energy transport has a largely gyro-Bohm like behaviour. In the outer region, however, trace T confinement shows a Bohm like behaviour in line with the analysis of earlier JET experiments [5]. The ρ^* scans for energy transport were performed in Type I and Type III ELMy H-mode plasmas, with the Type I scan found to be significantly affected by the variation in heating profile across the scan. The resulting variation in temperature profile indicates that the plasmas were in a region of non-stiff transport. It should be noted that $L_T = T/\nabla T$ was in excess of 7cm in all cases. Trace T confinement is found to have a positive dependence on β with an even stronger positive dependence seen in the wider fit. A similar impact of β on trace helium confinement has been

observed at DII-D [10]. The effect of β on energy confinement is found to be negligible in all three dedicated scans, even when the scan was solely within Type I ELMs. The local core energy transport is also found to be β independent. In the two point v^* scan, trace T transport is found to be moderately positively dependent on v^* , although the wider fit indicates a weaker dependence. In the energy transport experiment, energy confinement was seen to decrease weakly with increasing v^* .

For energy transport, the essentially gyro-Bohm like dependence of IPB98(y,2) is thus well verified by the JET ρ^* scans in both Type I and Type III ELMy H-modes. The negligible v^* dependence of IPB98(y,2) is contradicted somewhat by the dedicated scan, however, where a moderate negative effect was observed. More extremely, the strongly negative β scaling of IPB98(y,2) has been contradicted by all dedicated β scans, which all show an almost negligible β dependence. Applying the IPB98(y,2) scaling to trace T transport, it can be seen that its ρ^* scaling is broadly in agreement with the dedicated scan and the wider fit, but with some evidence of a weaker Bohm-like behaviour in the outer ($x=0.65-0.85$) region. The dedicated v^* scan indicates a somewhat stronger and positive effect on trace T confinement, although this was not born out by the wider fit. The β dependence of both the dedicated scan and the wider fit, however, shows a moderate to strong positive effect of β on trace T confinement in contrast to both IPB98(y,2) and the dedicate energy transport β scans. The observation that $D/\chi=0.3-1.5$, contradicts a single particle-energy transport scaling, as in (1b).

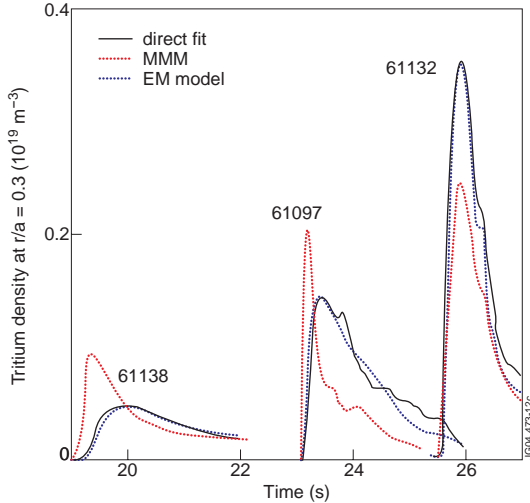


FIG. 11. Evolution of T density ($r/a = 0.3$) for three discharges using the fitting method of section 2 (solid black), MMM model (dotted red) and an EM model [11] (dashed blue). A time shift of 3s is used for discharge 61132.

Electrostatic models, such as the MMM (FIG. 11), are not consistent with the observed β dependence of trace T confinement, but a model based on neoclassical particle orbits in stochastic electromagnetic fields [11] has been shown to be consistent (FIG. 11). However, as the dimensionless scans have demonstrated a weak to negligible β scaling for energy transport, it may be postulated that the energy channel is dominated by electrostatic transport. The energy confinement scaling law derived from the ITPA multi-machine database, may be made consistent with this by performing a log-linear regression with both the Kadomtsev and electrostatic constraint imposed. The resulting fit to DB3v5 is

$$\tau_{ES} = 4.87 \times 10^{-2} \cdot P_{loss}^{-0.55} B_0^{0.09} I_p^{0.72} \kappa_a^{0.74} \bar{n}_e^{0.51} a^{0.78} R^{1.36} M^{0.10}, \quad (7)$$

which has the dimensionless form $B_0 \tau_{ES} \propto \rho^{*-2.8} \beta^{0.0} v^{*-0.09}$. This has a close to gyro-Bohm scaling, in agreement with the ρ^* scans of section 3, but a weaker v^* dependence than for the dedicated v^* scan (N.B. several alternate scalings [10, 4, 8, 12] show a similar weak or negligible β dependence). When applied to the ITER, $\beta_N=1.8$, $Q=10$ baseline point [1] the electrostatic scaling predicts a slightly higher energy confinement time, $\tau_{ES}=3.75s$, than IPB98(y,2), $\tau_{IPB98(y,2)}=3.67s$. At higher values of β_N , however, the electrostatic prediction

becomes significantly higher than that of IPB98(y,2) (e.g. 50% higher for $\beta_N=3.0$). The impact of this on ITER operation can be seen by comparing the plots of the ITER density and temperature operational space calculated with the IPB98(y,2) scaling (FIG. 12a) and with the electrostatic scaling (FIG. 12b). Although both scalings predict $Q \approx 10$ for the $\beta_N=1.8$, $n/n_{GDL} = 0.85$ point, for the IPB98(y,2) prediction Q falls with an increase in β_N at constant density and an increase in density to the Greenwald limit produces little increase in Q . By contrast, for the electrostatic scaling Q can be made to increase to $Q=15$ by increasing β_N above 1.8 and an even larger increase in Q can be achieved by increasing density. The trace T experiments indicate an associated unfavourable increase in particle confinement, and the effect of this on helium ash removal remains to be assessed.

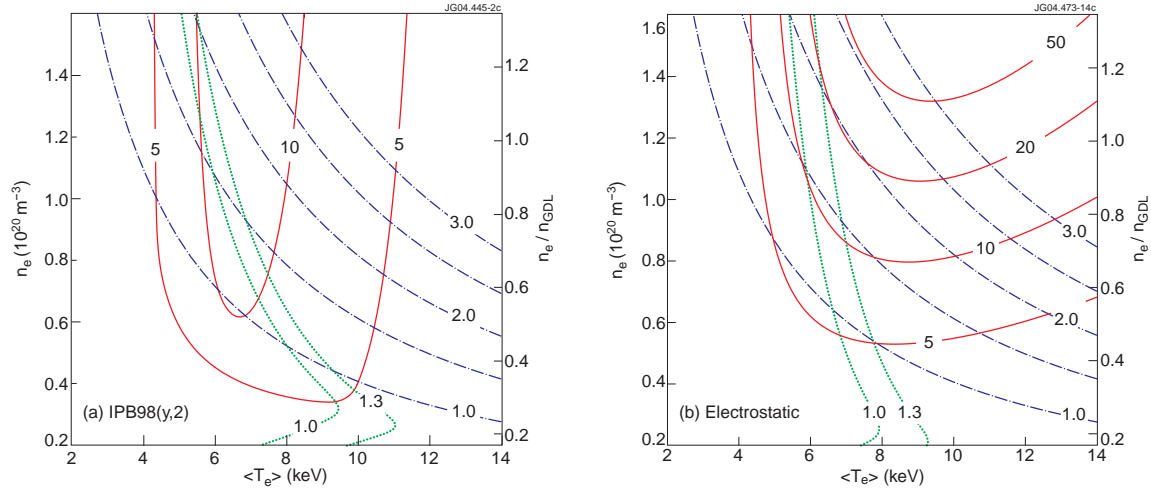


FIG. 12. POPCON plots of the ITER operation space in volume averaged density and temperature showing contours of fusion gain Q (red solid lines), normalised β (blue dashed and dotted line), and power relative to the L-H threshold (green dotted lines). Energy confinement is assumed to go as (a) IPB98(y,2), equation (1a), and (b) as in the electrostatic scaling of equation 7.

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